Static Analysis for High Level Programs Deliverable D2-2

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Abstract

This deliverable presents the static analyses developed during the VECOLIB project for the analysis of programs with containers. These analyses are based on abstract interpretation and specific abstract domains for set, multiset, and sequences containers.

1 Motivation and Related Work

Containers are general-purpose data structures for inserting, retrieving, removing, and iterating over elements. Examples of containers are array, list, vector, map, set, stack, queue, etc. They are widely used in client programs are therefore provided by common programming languages or standard libraries.

There are many different kinds of containers, varying in the convenience or efficiency of certain operations. However, from a point of view of the iteration operation, containers divide in two classes, as observed by Dilling et al [3]:

- position dependent containers where a position inside the container has a well-defined meaning and the iteration over its elements is done in a pre-defined order; such containers are array, vector, list, stack, and queue containers;
- value dependent containers where the iteration order may be undefined, for example set, multiset and map.

This classification captures the kind of properties could be specified on a container. Therefore, the position dependent properties like sorting for the first class, i.e., properties relating the values stored at different positions of the container:

 $\forall i_1, i_2 \in \text{positions}(c). \ i_1 \leq i_2 \Rightarrow \text{get}(c, i_1) \leq \text{get}(c, i_2),$

where i_1, i_2 are positions and c is the container for which accessing the value et some position is done using **get** function. For the value dependent containers, universal properties over values stored, e.g., all element greater than 5:

$$\forall i \in \texttt{positions}(c). \ \texttt{get}(c, i_1) \geq 5.$$

Another class of properties focus on relations between several containers, e.g., all values of the container c_1 are greater than the values stored by c_2 :

 $\forall i_1 \in \texttt{positions}(c_1), i_2 \in \texttt{positions}(c_2). \ \texttt{get}(c_1, i_1) \geq \texttt{get}(c_2, i_2).$

The verification of programs using containers, called client programs in the following, could require to deal with such constraints. Notice that, for position dependent containers, the class of properties as above involving positions related by complex constraints may not have a decidable satisfiability or entailment problems. A static analyser manipulating such constraints should either work on a decidable class of constraints or propose sound procedure for the decision problems required by the analysis.

In [3], Dillig et al proposes a static analysis based on a domain of indexed constraints to automatically infer properties on position or value dependent containers. Their domain has been implemented in the tool Compass and applied to the analysis of client programs using C++ libraries. The experimental results obtained demonstrate the good precision of the analysis proposed: more than 50% of false positives have been eliminated.

Another approach to represent constraints over containers has been proposed in [6] and it considers higher-order functional programs. It uses the Liquid Types framework [7] to reduce the safety of a functional program to the safety of a first-order imperative program. In this way, the safety of the functional program can be checked using any program analysis for imperative programs introduced in the literature.

2 Principles of Static Analyses

remove(c,v)

isin(c,v)

In general, a static analysis is built on (i) an abstract representation of sets of program configurations, where the set of values of this abstraction is called an abstract domain, and (ii) an encoding of the program statements in terms of abstract values transformations, also called abstract transformers.

We fix the set of operators a client program may call on a container depending on its kind: value or position dependent. The table below lists these operations are give their intuitive semantics.

	Position dependent
init()	creates the empty container
is_empty(c)	test for empty container
add_first(c,v)	push a value before the first position
add_last(c,v)	push a value after the last position
remove_first(c)	remove the value at the first position
remove_last(c)	remove the value at the last position
first_pos(c)	return the first position or -1
next_pos(c,p)	return the next position or -1
last_pos(c)	return the last position or -1
get_at(c,p)	return the value at a valid positon or nil
isin(c,v)	returns the position of the value in the container or nil
	Value dependent
init()	creates the empty container
is_empty()	test for empty container
add(c,v)	push a value

remove a value

For each kind of container, we define in the next sections an abstract domain and the

return true iff the value is in the container

abstract transformers for the above operators.

3 Abstract Domain for Sequences

Sequences are natural abstractions for the unbounded position dependent containers like vectors and lists. The abstract domain we propose is inspired from our previous work on the analysis of programs manipulating dynamic linked lists [1], where sequences where used as model for the heap content. The main difference with this previous work is the abstract transformers required on the sequence abstract domain. For programs using a low level manipulation of the heap, the operations on the sequence model where: split the sequence in a head value and the remaining of the sequence, add a value at the end of the sequence, concatenate two sequences. For the programs manipulation position dependent containers, we have to implement the operations in the table above including the ones concerning positions, which is a novelty w.r.t. the previous usage of this domain.

The abstract domain $\mathcal{A}_{\mathbb{S}}$ has as values special constraints over a set of variables consisting of:

- a set \mathcal{C} of position dependent containers,
- a set \mathcal{V} of integer variables,
- a set \mathcal{P} of positions variables (although in most of languages positions are usually integers, we keep them separate to relate easily valid positions), and
- a set $\mathcal{L}_{\mathcal{C}}$ of integer variables, one for each container variable in \mathcal{C} , that represent the size of the container.

The constraints stored have the following for:

$$(E \wedge \bigwedge_{G(\vec{y}) \in \mathcal{G}} \forall \vec{y}. \ G(\vec{y}) \Rightarrow U(\vec{y})), \text{ where}$$

- E is a value of a numerical abstract domain $\mathcal{A}_{\mathbb{Z}}$ (such as the Octagons abstract domain, the Polyhedra abstract domain [5], etc.) constraining the set of variables $\mathcal{V} \cup \mathcal{P} \cup \mathcal{L}_{\mathcal{C}}$. In is called the *existential part* of the abstract value.
- \vec{y} is a set of fresh *position variables* interpreted as integers representing positions in the sequences,
- \mathcal{G} is a set of guards $G(\vec{y})$, which belong to a specific set of patterns. From our experience with the analysis of client programs, we include in this set the following patterns (for any variable in \mathcal{C} :
 - $-y \in \text{positions}(s)$ which corresponds to a universal quantification over all the values in the sequence s,
 - $-y_1 \in \text{positions}(s_1) \land y_2 \in \text{positions}(s_2)$ which allows to compare the values of two containers,
 - $-y_1 \leq y_2 \in \text{positions}(s)$ which allows to express sorting properties, and
 - $-y_1 \in \text{positions}(s_1) \land y_2 \in \text{positions}(s_2) \land y_1 = y_2$ which allows to compare, position by position, the values of two sequences.

• $U(\vec{y})$ is a value in a numerical abstract domain $\mathcal{A}_{\mathbb{Z}}$ constraining the set of variables get(s, y), denoting the integer at position y in the sequence s, len(s), and get(s, 0). A term s[y] appears in $U(\vec{y})$ only if the guard $G(\vec{y})$ contains a constraint $\vec{y} \in positions(s)$. This restriction is used to avoid undefined terms. For instance, if s denotes a sequence of length 2 then the term get(s, y) with y interpreted as 3 is undefined.

For example, the following abstract value represent configurations of a position dependent container c which has length less than ℓ and it is sorted:

$$len(c) < \ell \land \forall y_1 \le y_2 \in positions(c) \Rightarrow get(c, y_1) \le get(c, y_2)$$

To define the abstract transformers implementing the container operations, we use the basic operations described in [4, 2] for the domain of sequences:

- lattice operations: built top \top and bottom \bot abstract values, test inclusion of abstract values $a_1^{\sharp} \sqsubseteq a_2^{\sharp}$,
- widening of two abstract values $a_1^{\sharp} \nabla a_2^{\sharp}$,
- in an abstract value a^{\sharp} , split a sequence s after the position p to obtain new sequences s_h and s_t , $\text{split}(a^{\sharp}, s, p, s_h, s_t)$,
- in an abstract value a^{\sharp} , fold a sequence of sequence variables $[s_1, \ldots, s_n]$ into a sequence variable s (for existential quantifier elimination), $\texttt{fold}(a^{\sharp}, [s_1, \ldots, s_n], s)$.

We also define the following new basic operations:

• built a sequence s of one value v, $newunit(a^{\sharp}, s, v)$.

Using the above basic operations, the abstract transformers for operations on containers are defined as follows:

- init(c) introduces a new constraint for the container assigned in the existential part: len(c) = 0,
- is_empty(c) intersects the abstract value with the constraint len(c) = 0 and returns true iff the value obtained is not empty (i.e., the constraint is still satisfiable).
- add_first(c,v) applies first newunit(a[♯], s, v) to obtain a[♯]₁, then applies folding fold(a[♯]₁, [s, c], c).
- add_last(c,v) applies first newunit(a[♯], s, v) to obtain a[♯]₁, then applies folding fold(a[♯]₁, [c, s], c).
- remove_first(c) applies splitting at position 0, $split(a^{\sharp}, c, 0, c_h, c)$, and the value of c_h is bound to the result of the operation.
- remove_last(c) applies splitting at position len(c) 2, $split(a^{\sharp}, c, len(c) 2, c, c_l)$, and the value of c_l is bound to the result of the operation.
- first_pos(c) applies emptiness test and if it returns false then returns 0.

- next_pos(c,p) intersects with the constraint len(c) > p+1 and is the obtained abstract value is not empty, sets the results to p + 1; otherwise returns -1.
- last_pos(c) applies emptiness test and if it returns false then returns len(c) 1.
- get_at(c,p) intersects with the constraint len(c) > p >= 0 and if it returns an non empty abstract value, then applies $split(a^{\sharp}, c, p-1, c_h, c_t)$, and constrains the the result to be equal to $get(c_t, 0)$.
- isin(c,v) generates a set of four possible abstract values depending on the position of the value v: at the first resp. last position, in the middle of c or never present in c. Notice that the abstract transformer for this operation is not very precise because we can not represent inside the abstract values negative assertions.

4 Abstract Domain for Multisets

The abstract domain $\mathcal{A}_{\mathbb{M}}$ has as values special constraints over a set of variables consisting of:

- a set \mathcal{C} of position dependent containers,
- a set \mathcal{V} of integer variables,
- a set \mathcal{P} of positions variables (although in most of languages positions are usually integers, we keep them separate to relate easily valid positions), and
- a set $\mathcal{L}_{\mathcal{C}}$ of integer variables, one for each container variable in \mathcal{C} , that represent the size of the container.

The constraints stored have the following for:

$$\left(E \land \bigwedge_{G(\vec{y}) \in \mathcal{G}} \forall \vec{y}. \ G(\vec{y}) \Rightarrow U(\vec{y})\right), \land \left(\bigwedge_{i} t_{1}^{i} = t_{2}^{i}\right) \text{ where }$$

• t_1^i, t_2^i are multiset terms of the form $u_1 \cup \cdots \cup u_s$ $(s \ge 1 \text{ and } \cup \text{ is the union of multisets})$ where basic terms u_i are of the form (1) mshd(n) (resp. d) representing the singleton containing the first integer of the sequence labeling n (resp. the value of d), or (2) mstl(n) representing the multiset containing all the integers of the sequence n except the first one. As a shorthand, $\text{mhd}(n) \cup \text{mtl}(n)$ is denoted by ms(n).

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